

ASSIGNMENT – 1(MATHEMATICS)

CLASS – 8

Copy the notes in your maths copy and then do the homework in the same copy.

CHAPTER - 5

PLAYING WITH NUMBERS

Generalized form – A number is said to be in generalized form, if it is expressed as sum of the products of its digits with their respective place values.

Example of 2 digit number – 34, 56, 78 etc.

34 can be written as –

$$34 = 30 + 4 = 10 \times 3 + 4$$

In general, a 2-digit number ab can be written as

$$ab = 10 \times a + b = 10a + b$$

Similarly, $ba = 10 \times b + a = 10b + a$

Example of 3 digit number – 456, 789, 967 etc.

456 can be written as –

$$456 = 400 + 50 + 6 = 100 \times 4 + 10 \times 5 + 6$$

In general, a 3-digit number abc can be written as

$$abc = 100 \times a + 10 \times b + c$$

Similarly, $bca = 100 \times b + 10 \times c + a$

and $cab = 100 \times c + 10 \times a + b$

So the number ab does not mean $a \times b$

And the number abc does not mean $a \times b \times c$

Example 1 – write 287 in generalized form

$$\begin{aligned}\text{Solution – } 287 &= 2 \times 100 + 8 \times 10 + 7 \times 1 \\ &= 2 \times 100 + 8 \times 10 + 7\end{aligned}$$

- Reversing the digits of a 2-digit number

Let us consider a 2-digit number 37

Reverse the digit, we get a new number i.e. 73

Adding new number to the original number, we get

$$37 + 73 = 110$$

Thus, $110 = 11 \times 10$, the number is divisible by 11 and also by 10 which is the sum of the digits i.e. $3 + 7 = 10$

Check:-

Consider any 2-digit number ab i.e. $10a + b$

Reverse the digit ab to get a new number ba i.e. $10b + a$

Adding these numbers, we get

$$(10a + b) + (10b + a) = 11a + 11b = 11(a + b)$$

Hence, the sum of original number and the number which we obtained by reversing the number is always divisible by 11 and sum of the digits i.e. $(a + b)$

- Consider another 2-digit number 68

Reverse the digit to get a new number i.e. 86

Subtracting the greater number to the smaller one, we get

$$86 - 68 = 18$$

Thus, the difference $18 = 9 \times 2$, which is divisible by 9 and also by 2 which is the difference of the digits i.e. $8 - 6 = 2$

Check:-

Consider any 2-digit number ab ($a > b$) i.e. $10a + b$

Reverse the digits ab to get a new number ba i.e. $10b + a$

Subtracting larger number to the smaller number, we get

$$(10a + b) - (10b + a) = 9a - 9b = 9(a - b)$$

So, it is always divisible by 9 and the difference of the digits i.e. (a-b)

Example 2 – write the quotient when the sum of a 2-digit no. 27 and number obtained by reversing the digits is divided by

(i) 11

(ii) sum of digits

Solution: Given no. = 27

By reversing the given number,
we get a new number = 72

$$\text{Sum} = 27 + 72 = 99 = 11 \times 9$$

(i) if it is divided by 11, quotient is 9

(ii) sum of digits = $2 + 7 = 9$

Therefore, when sum 99 is divided by 11, quotient is 9

Example 3 – In two digit number, the unit digit is 3 times the tens digit and sum of the digits is 12. Find the number.

Solution – Let unit's digit = a

Ten's digit = b

$$a = 3b \quad \text{----- (1)}$$

$$a + b = 12 \quad \text{----- (2)}$$

Putting the value of a from equation (1) to equation (2)

$$3b + b = 12$$

$$4b = 12$$

$$b = 3$$

put the value of b in equation (1)

$$a = 3 \times 3 = 9$$

$$\text{the number} = 10b + a = 10 \times 3 + 9 = 30 + 9 = 39$$

Example 4 – the sum of the digits of a 2-digit number is 11. The number obtained on reversing its digits is 27 more than the original number. Find the original number?

Solution – let ten's place = a, unit's place = b

$$a + b = 11 \quad \text{----- (1)}$$

$$\text{Number} = 10a + b$$

$$\text{Reversing the number} = 10b + a$$

From condition

$$10b + a = (10a + b) + 27$$

$$10b + a - 10a - b = 27$$

$$9b - 9a = 27$$

$$9(b - a) = 27$$

$$b - a = 3 \quad \text{----- (2)}$$

By elimination method,

$$b + a = 11$$

$$b - a = 3$$

$$2b = 14$$

$$b = 7$$

$$a = 11 - b = 11 - 7 = 4$$

So, the required number is $10a + b = 10 \times 4 + 7 = 40 + 7 = 47$

Home work :

Exercise 5.1 question no. 1, 2, 3, 6, 7, 8